SRNL Technical Work Scope for the Hydrogen Storage Engineering Center of Excellence

Design and Testing of Metal Hydride and Adsorbent Systems

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Savannah River National Laboratory
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This presentation does not contain any proprietary, confidential or otherwise restricted information
Overview

Timeline
• Start: February 1, 2009
• End: July 31, 2014
• 20% Complete (as of 3/31/10)

Budget
• FY 09 Funding: $888,945*
• FY10 Funding: $1,640,000*

* Includes $241,200/$360,000 for the University of Quebec Trois Rivieres (UQTR) as a subrecipient for FY09/FY10

Barriers
• System Weight and Volume
• H₂ Flow Rate
• Energy Efficiency

Partners
Transport Phenomena provides the modeling and analysis required for prototype design, along with interpretation and scaling of prototype data.
Relevance: Phase 1 Objectives – Transport Phenomena

- Collect and Assimilate Property Data for Metal Hydrides and Adsorbents
  a. Kinetics data and kinetics models
  b. Thermal and mass transport data
  c. Evaluate completeness of available data
  d. Propose experiments to obtain missing data
  e. Interface with MHCoE and independent projects

- Collect Operational Data for Storage Vessel Configurations
  a. Heat transfer
  b. Mass transfer
  c. Identify additional data required

- Develop General Format for Models
  a. Suitable for sensitivity/scoping studies and detailed analyses
  b. Metal hydrides and adsorbent models to be developed by SRNL/UQTR
  c. Chemical hydride models to be developed by PNNL and LANL

- Assemble and Test Models
  a. Conduct preliminary validation

- Develop “Acceptability Envelope” of Media Characteristics Based on 2010 & 2015 DOE Technical Targets
  a. Determine whether candidate metal hydrides have characteristics lying within the “acceptability envelope”

Principal Objectives:
- Development of an “Acceptability Envelope” for metal hydride properties
- Develop numerical models for system optimization and sensitivity studies
Approach: Modeling Hierarchy

1. **DOE Technical Targets**
2. **Media kinetics/isotherm data**
3. **Media thermal and transport property data**
4. **Acceptability Envelope**
5. **Integrated storage system models (3D, 2D, sensitivity/scoping)**
6. **Vehicle system models**
7. **Storage system design concepts**
8. **Prototype designs**
9. **Prototype data**
10. **Test matrix for prototype experiments**
11. **Data interpretation using integrated models**
12. **Prediction of full-scale storage system behavior using integrated models**

**Transport Phen. Technology Area**

**Ultimate HSECoE Goal**
Technical Accomplishments: 0-D MathCAD® Kinetics Model for Metal Hydrides

UTRC Prototype 2

Kinetics

Hydride: NaAlH₄ + 2% TiCl₃x1/3AlCl₃+0.5% FeCl₃

Mass H₂ Stored
- 5.5 kg in 4.2 min (2010 Target)
- Includes compressed gas in voids (~50% porosity)

Total Tank Volume: 0.32 m³
- 4 Tanks
  - Length: 4 ft (1.2 m)
  - Diameter: 1 ft (0.3 m)

Discharge Conditions:
- Pressure: 4 bar
- Temperature: 170 ℃

ΔT is used in the “Acceptability Envelope”

2010 target charging time

ΔT ≈ 30°C
**Approach: Physics for Integrated Metal Hydride Models**

**Conservation of Mass (Hydrogen)**
\[
\frac{\partial C}{\partial t} + \nabla \cdot (C \vec{v}) = \left( \frac{S_{H_2}}{\varepsilon} \right)
\]

**Conservation of Momentum**
(Blake-Kozeny Equations)
\[
\begin{align*}
u &= -\frac{D_p}{150\mu} \left( \frac{\varepsilon}{1-\varepsilon} \right)^2 \frac{\partial P}{\partial x} \\
v &= -\frac{D_p}{150\mu} \left( \frac{\varepsilon}{1-\varepsilon} \right)^2 \frac{\partial P}{\partial y} \\
w &= -\frac{D_p}{150\mu} \left( \frac{\varepsilon}{1-\varepsilon} \right)^2 \frac{\partial P}{\partial z}
\end{align*}
\]

**Conservation of Energy in Bed**
\[
\rho_{bed} C_{p_{bed}} \frac{\partial T}{\partial t} - \nabla \cdot k \nabla T = -\varepsilon \rho_{H_2} C_{p_{H_2}} \left( \frac{\partial T}{\partial t} + \vec{v} \cdot \nabla T \right) - \left( \sum_i \left[ \frac{1}{M_i} \frac{\partial \rho_i}{\partial t} \Delta H_i \right] \right)
\]

\[
\frac{dC_1}{dt} = \begin{cases} 
\frac{3C_2(t)}{C_{eqv}} - C_{2sat}(T) & \text{if } P \geq P_{eq_{q_1}}(T) \\
C_1(t) & \text{if } P < P_{eq_{q_1}}(T) \text{ and } C_1(t) \geq 0
\end{cases}
\]

\[
\frac{dC_2}{dt} = \begin{cases} 
\frac{3C_2(t)}{C_{eqv}} - C_{3sat}(T) & \text{if } P \geq P_{eq_{q_2}}(T) \\
\frac{C_2(t)}{C_{eqv}} & \text{if } P < P_{eq_{q_2}}(T) \text{ and } C_2(t) \geq 0
\end{cases}
\]

**Plus Non-Ideal Hydrogen Equations of State and Transport Properties, Material Property Correlations, Correlations for Physical Processes, Ancillary Equations, etc. !!!**
Approach: Sample Geometric Representation - Metal Hydride Model

This is a specific example. The generalized FEM model can be applied to any geometry and set of thermal properties.

Sample Cross-Section Schematic

Sample Geometry Used in 3-D Model

Sample Geometric Parameters

- Diameter 23.0 cm
- Length 68.90 cm
- Fin Thickness 0.0313 cm
- Axial Spacing of Fins 0.64 cm
Approach: Unit Cell Model for Heat Removal Scoping Studies

Symmetry assumed
- Each tube independent
- End effects neglected (Assumed 2-D)
- Axially symmetric

Spatially uniform H₂ pressure assumed

Explicit representation of fin and tubes

Media-metal thermal contact resistances explicitly included

Conditions (Adjustable)
- NaAlH₄ + 4%TiCl₃ kinetics parameters
- 50 bar H₂ feed pressure
- 100 °C cooling fluid

Optimized Parameters (Use Matlab®-Comsol® Interface)
- Cooling tube (inner) diameter
- Cooling tube thickness
- Tube (horizontal) spacing
- Fin thickness
- Fin-Fin (vertical) spacing

Grid or Nelder-Mead (Downhill Simplex) Optimization
Technical Accomplishments: Systematic Optimization Method

Store 1 kg of hydrogen in 12 min. (720s) 50 bar feed pressure; NaAlH₄+4%TiCl₃

Nelder-Mead

- Cooling tube ID: 0.085 in
- Cooling tube thickness: 0.020 in
- Fin length: 0.296 in
- Fin thickness: 0.004 in
- Fin-Fin spacing: 0.220 in

Number of units: 126050
Media mass: 126 kg
Heat exchanger mass: 17 kg
Heat exchanger vol. %: 3.4%

Temperature (°C)

Stored Hydrogen (kg/m³)
Technical Accomplishments: Novel Concepts

**Longitudinal Fins**

Symmetry assumed
- Each tube independent
- End effects neglected (Assumed 2-D)
- 60° wedge

Spatially uniform H₂ pressure assumed

Explicit fin and tubes

Media-metal thermal contact resistances included

Conditions (Adjustable)
- 50 bar H₂ feed pressure
- 100 °C cooling fluid

**Advantages**
- Media Packing

**Disadvantages**
- Construction Cost

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**Metallic Honeycomb Structure**

Thickness \( t \) (in) | 0.04
--- | ---
Cell size \( l \) (in) | 1/2

- Symmetry assumed (30°)
- Axial hydrogen injection at 50 bar
- Contact resistance not considered
Progress: Summary and Current Results for Metal Hydrides

Developed and validated baseline Comsol® models for metal hydride storage systems

Incorporated improved models into optimization routines

- With given constraints optimal designs require very small spacing of HX surfaces
- Methods easily extendable to new systems
  - New hydrides
  - New catalysts for NaAlH₄
  - Adsorbent systems
  - New tank designs

Principal issues for design of metal hydride based storage systems

- Variations in powder composition and catalyst material
  - Large impact on the charging and discharging kinetics
  - Large impact on capacity

- Substantial increase (x50) in NaAlH₄ kinetics required to meet 2010 DOE target for refueling time
  - Heat removal becomes an issue for ΔH associated with most metal hydrides

- Short refueling times for NaAlH₄ (e.g., 4.2 min. versus 15 min) impact
  - System gravimetric capacities
  - System volumetric capacities
Proposed Future Work: Metal Hydrides

**More Detailed Modeling in Scoping Studies**
- Consider mass transfer limitations
- Include hydrogen stored in gas phase
- Include cooling at tank wall/surface
- Identify minimum coolant tube thickness
  - Dependent on operating pressure and tube internal diameter
- Use appropriate convection heat transfer coefficient in coolant tube
  - Dependent on coolant tube internal diameter & coolant flow rate
- Consider pressure vessel mass
  - Important for hybrid (high pressure) storage

**Evaluate Novel Concepts**
- Longitudinal and other fin configurations
- Metal honeycomb structures
  - Cell size
  - Addition of cooling channels

\[
\begin{align*}
    u &= -\frac{D_p^2}{150\mu\left(1 - \varepsilon\right)^2} \frac{\partial P}{\partial x} \\
    v &= -\frac{D_p^2}{150\mu\left(1 - \varepsilon\right)^2} \frac{\partial P}{\partial y} \\
    w &= -\frac{D_p^2}{150\mu\left(1 - \varepsilon\right)^2} \frac{\partial P}{\partial z}
\end{align*}
\]
Approach: Adsorbent Models – MaxSorb® (AX-21®)

- **Solves conservation equations for mass, momentum, and energy in 2 or 3 dimensions**
  - Uses weakly compressible Brinkman equations in all flow domains
    - Includes thermal radiation
  - Temperature dependent fit for carbon specific heat
  - Correlations for non-ideal hydrogen properties from NIST REFPROP 23 V8.0 database
    - Valid for $0.05 \leq P \leq 35.0\text{MPa}$ and $70 \leq T \leq 450\text{K}$
    - Compressibility factor
    - Enthalpy
    - Viscosity
    - Thermal conductivity

- **AX-21® thermodynamic models for absolute adsorption and internal energy of adsorbed hydrogen obtained from:**
Technical Accomplishments: Adsorbent Scoping Model

- **Unit cell**
  - Half-thickness of fin & media
  - Central coolant channel

- **Energy balance only**
  - Prescribed pressure transient

- **Executes quickly**
  - Analogous to SRNL heterogeneous cell metal hydride scoping models
  - Suitable for large number of runs
    - Matlab<sup>®</sup> systematic optimization on a number of design parameters

- **Optimized Parameters (Use Matlab<sup>®</sup>-Comsol<sup>®</sup> Interface)**
  - Cooling tube (inner) diameter
  - Cooling tube thickness
  - Tube (horizontal) spacing
  - Fin thickness
  - Fin-Fin (vertical) spacing
Technical Accomplishments: Model Validation

- Model uses properties of structures and thermocouple materials at cryogenic temperatures
- Thermocouple composition reflects that in experimental apparatus
Technical Accomplishments: Model Validation

Total Hydrogen Concentration (mol/m$^3$) During Loading

$P_0=0.182$ MPa

$100$ Seconds

$P=0.372$ MPa

$800$ Seconds

$P=2.228$ MPa

$1600$ Seconds

$P=4.938$ MPa
Technical Accomplishments: Model Validation

**TC 1 Temperatures**

**TC 2 Temperatures**

**Average Bed Temperatures (not including structures or thermocouples)**

**Effect of Bed Thermal Conductivity**

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**Graphs showing model validation:**
- TC 1 and TC 2 Temperatures with data, refined model, and original model.
- Average bed temperatures highlighting data, refined model, and original model.
- Effect of bed thermal conductivity with different model variations.
Progress: Summary for Adsorbent Modeling

• **Model Development and Validation**
  - Numerical model – Comsol®
  - Model validation against data for MaxSorb®

• **Developed Baseline Scoping Model**
  - Unit cell models – Comsol®
Proposed Future Work: Adsorbent Models

- Conduct validation experiments that reduce parasitic heat transfer
  - Use N₂ at temperatures closer to ambient
- Compare performance of MOF-5® and MaxSorb®
- Use baseline models in 2 and 3 dimensions for design and sensitivity studies
  - Vessel design
  - Structured media
  - Novel concepts
- Conduct process-specific experiments
  - Validate models
  - Test conceptual vessel designs
- Convert models to a form suitable for use in system analysis
- Apply models to prototype design
Approach: Acceptability Envelope

• The “Acceptability Envelope” or “Black Box Analysis” determines the range of parameters necessary for a coupled media and system to meet storage system performance targets
  - Based on energy balance
  - Serves as media screening tool
    - *Guide for material development*
  - Uses technical targets to establish values for parameter “grouping”
    - *Defines ranges of parameters for media & storage vessel*
• Current analysis applied to metal hydrides
  - Rectangular coordinates (RC)
  - Cylindrical coordinates (CC)
Technical Accomplishments: Acceptability Envelope

For both rectangular and cylindrical geometries

\[ \Delta T = -\frac{1}{m} \left[ \frac{L^2}{k} \Delta H_{\text{overall}} \frac{\rho_{\text{Hydride}}}{M_{\text{Hyd}_\text{eff}} M_{\text{H}_2}} \frac{\Delta m_{\text{H}_2}}{\Delta t} \right] \]

\[ \Delta T = T_{\text{max}} - T_{\text{min}} \]

\[ L^2 = r_1^2 - r_2^2 \] \text{cylindrical}

\[ L = (\text{plate spacing}) \] \text{rectangular}

Rearrange to get

\[ \left( \frac{1}{L^2} \right) \left( \frac{k \ M_{\text{Hyd}_\text{eff}} \Delta T}{-\Delta H_{\text{overall}} \rho_{\text{Hydride}}} \right) = \frac{1}{mM_{\text{H}_2}} \frac{\Delta m_{\text{H}_2}}{\Delta t} \]

Linear relation between charging/discharging rate and media and system parameters

Currently assumes recoverable hydrogen is stored in metal hydride - OK for moderate pressures

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>L</td>
<td>Distance between heat transfer surfaces</td>
</tr>
<tr>
<td>( \Delta T )</td>
<td>Temperature range for acceptable chemical kinetics (to give charge/discharge rate of ( \Delta m_{\text{H}_2}/\Delta t ))</td>
</tr>
<tr>
<td>( M_{\text{Hyd}_\text{eff}} )</td>
<td>Mass of hydride (in reference form) required to load target amount of hydrogen in specified time (relates to kinetics)</td>
</tr>
<tr>
<td>( \Delta H_{\text{overall}} )</td>
<td>Overall heat of reaction</td>
</tr>
<tr>
<td>( \rho_{\text{Hydride}} )</td>
<td>Hydride density (in reference form)</td>
</tr>
<tr>
<td>( k )</td>
<td>Bed thermal conductivity</td>
</tr>
<tr>
<td>( \Delta m_{\text{H}_2}/\Delta t )</td>
<td>Required rate of charging/discharging from DOE Technical Targets</td>
</tr>
</tbody>
</table>
Technical Accomplishments: Application of Acceptability Envelope

NaAlH₄ System:
Minimum Required Bed Thermal Conductivity (in W/m K)
(RC, wall fixed T, ρ=720 kg/m³, ΔL=0.0127 m, ΔH=40.3 kJ/molH₂)

ΔT=30°C
ΔL is distance between HX surfaces

If reactions are fast enough to meet target charging times, a high rate of heat removal is required
⇒ Close spacing of HX surfaces
or
⇒ Higher value of k

Alternatives:
Reduce ΔH_{overall}
Increase ΔT_{max}

DOE 2010 ★ ★ 5kg H₂ in 4.2 min
DOE 2015 ★ ★ 5kg H₂ in 3.3 min
Progress: Summary for Acceptability Envelope

• **Model Developed for Metal Hydrides**
  - Based on energy balance
    - Constraints are from DOE Technical Targets
    - Model should be used in conjunction with media kinetics
  - Can be used to identify range of media & component parameters required to meet operational targets

• **Application**
  - Applied to NaAlH$_4$
  - Some general applications have been made
Proposed Future Work: Acceptability Envelope

- **Include effects of system parameters**
  - Mass & volume of storage vessels, fins, tubes, other structures and fittings

- **Complete the application to metal hydrides**
  - Include coupled parameter ranges
  - Evaluate candidate metal hydrides

- **Develop and apply model for adsorbents**
Collaborations

• **Metal Hydride Modeling**
  - Mikhail Gorbounov, Daniel Mosher, Bart van Hassel (UTRC)
  - Jacques Goyette, Maha Bhouri (UQTR)
  - Sudarshan Kumar (GM)
  - Kevin Drost, Goran Jovanivich, Anna Garrison (OSU)

• **Adsorbent Modeling**
  - Richard Chahine, M. A. Richard (UQTR)
  - Andrea Sudik (Ford)
  - Sudarshan Kumar (GM)

• **Technology Area Interfaces**
  - Scot Rassat, Kriston Brooks, Ewa Ronnebro, Dale King (PNNL)
  - Troy Semelsberger (LANL)
  - Norman Newhouse (Lincoln Composites)
  - Joseph Reiter (JPL)
  - Donald Siegel (U of M)
Project Summary

Relevance
The ultimate goals of the HSECoE are the design and testing of prototype hydrogen storage vessels, the interpretation of test data and the implication for full scale vessels. Within the HSECoE, the Transport Phenomena Technology Area is responsible for the development and application of analyses for storage systems that are necessary to identify and design prototype media and vessel configurations having the best performance relative to the DOE Technical Targets. Storage vessel models developed by this technology area will be essential to interpret data obtained from prototype testing and to relate it to full scale systems.

Approach
In Phase I the Transport Phenomena Technology Area will:
- Evaluate, interpret, and assimilate data for media and vessel components
- Develop and apply an “Acceptability Envelope” to metal hydrides
- Develop general models for scoping and detailed evaluation of storage system designs
  - Validate and test the models

Technical Accomplishments and Progress (as of 3/2010)
Have met/exceeded Phase I objectives:
- Evaluated and interpreted media and component data; assimilated into models
- Developed and applied the “Acceptability Envelope” to metal hydrides
  - Applying to metal hydride vessel-media configurations
  - Developing model for adsorbents
- Developed baseline models for metal hydrides and adsorbents
  - Validated and tested the metal hydride models
  - Initiated validation of adsorbent model
  - Performed optimization studies of vessel configuration for NaAlH₄
  - Ready to compare storage system behavior for different media
    - Metal hydrides in general
    - Adsorbents MOF-5® and MaxSorb®

Collaborations
UQTR, UTRC, PNNL, LANL, JPL, Ford, GM, OSU, Lincoln Composites, U of M – (see previous slide)

Proposed Future Work (Phase I)
- Continue vessel optimization using models
  - Apply to novel design concepts
    - Micro & mini channel heat exchangers
    - Structured media
  - Develop and test models for adsorbents
- Extend “Acceptability Envelope” to adsorbents and apply
  - Include gravimetric and volumetric constraints
- Preliminary prototype designs
QUESTIONS
SUPPLEMENTAL SLIDES
Technical Accomplishments: Metal Hydride Models

• **Model Development and Validation**
  - 0-D kinetics model – MathCAD®
  - Baseline numerical model – Comsol®
  - Model validation against data

• **Optimization Studies**
  - Unit cell models – Comsol®
  - Results
  - Materials Requirements

• **Novel Concepts**
  - Assessment
Technical Accomplishments: 0-D MathCAD® Kinetics Model

Example: \( \text{NaAlH}_4 + 4\% \text{TiCl}_3 \)

UTRC kinetics and saturation parameters

Assumptions:
- Isothermal
- Isobaric
- Kinetic limitations only

Results
- Feed at 100 bar \( \text{H}_2 \) yields a significantly larger optimum temperature range
- \( \text{Na}_3\text{AlH}_6 \) saturation term reduces rate of formation of \( \text{NaAlH}_4 \)
- Saturation weight fraction controls optimal temperature

Optimum Temperature Range

Hydride Required to Store 1kg \( \text{H}_2 \) in 720s

![Graph showing the relationship between mass of hydride and \( \text{H}_2 \) bed temperature for different pressures (50 bar and 100 bar).](image-url)

![Graph showing the relationship between \( C_{1, \text{set}} \) and temperature.](image-url)
Kinetics Comparison

Saturation Weight Fraction

Fill Time at 200 bar Feed Pressure

- Prototype 1 Kinetics
- Prototype 2 Kinetics
Technical Accomplishments: Fill Time - Metal Hydride (NaAlH₄)

**UTRC Prototype 1 Kinetics**

**Hydride:** NaAlH₄ + 4%TiCl₃

**Mass H₂ Stored**
- 5.5 kg in 4.2 min (2010 Target)
- Includes compressed gas in voids (~50% porosity)

**Total Tank Volume:** 0.32 m³
- 4 Tanks
  - Length: 4 ft (1.2 m)
  - Diameter: 1 ft (0.3 m)

**Discharge Conditions:**
- Pressure: 4 bar
- Temperature: 170 °C
Technical Accomplishments: NaAlH₄ Kinetics Vs Storage Vessel Charge Rate

Coolant and Feed Hydrogen Temperatures Fixed at 100°C

Charging Pressure of 50 bar

Initially 13,333.33 mol/m³ of NaH 0 mol/m³ of NaAlH₄ and Na₃AlH₆

For Good Heat Transfer with NaAlH₄, Charge Rate Is Limited by Kinetics

![Transient Bed Loading](image-url)
Technical Accomplishments: Metal Hydride Model Validation (UTRC)

Comsol® model validated successfully by UTRC with ABAQUS® model and experimental data from previous DOE contract
Store 1 kg of hydrogen in 12 min. (720s)
50 bar feed pressure; NaAlH$_4$+4%TiCl$_3$

Nelder-Mead

Cooling tube ID: 0.085 in.
Cooling tube thickness: 0.020 in.
Fin length: 0.313 in.
Fin thickness: 0.004 in.
Linear length: 643 m
Media mass: 126 kg
Heat exchanger mass: 16 kg
Heat exchanger vol. %: 3.2%
Technical Accomplishments: Preliminary Scoping - Effect of Tube Arrangement on H₂ Charging

For the 2D models (cases a – d), increasing the number of heat exchanger tubes results in better utilization of the bed (higher H₂ loading rates).

No improvement is seen between 49 and 81 cooling tubes (cases c and d, respectively)

- Suggests the existence of an optimum number of cooling tubes.
Technical Accomplishments: Metallic Honeycomb Structure

- Decreasing the cell size results in a decrease of the maximum of temperature from 220 to 203°C
- No significant improvement on the bed weight fraction
- Adding a cooling jacket will improve the hydrogen loading rate
Technical Accomplishments: Acceptability Envelope Development

- **Geometry and boundary conditions**
  - Rectangular coordinates (RC)
  - Cylindrical coordinates (CC)
  - Different boundary conditions
    - Fixed wall temperature
    - No heat flux at wall

- **Criteria and media**
  - DOE technical targets
    - 2010, 2015 and Ultimate
  - Storage materials (NaAlH₄) current characteristics
Technical Accomplishments: Acceptability Envelope Derivation
Physical Model in Rectangular Coordinates

Steady-State Energy Balance

\[ k \frac{d^2T}{dx^2} + q''' = 0 \]

\( q''' \) (\( W/m^3 \)) is the rate of thermal energy release during charging or discharging.

\[ q''' = -\sum_i \Delta H_i \frac{\Delta C_i}{\Delta t} \quad \text{where:} \]
\( \Delta H \) (J/mol) is the enthalpy of reaction.
\( C_i \) (mol/m³) is concentration of H₂ stored by species i.
\( C_f \) (mol/m³) is overall concentration of stored H₂.
\( M_{\text{Hyd eff}} \) is the mass of hydride needed to store the required mass of hydrogen.

Solving the Energy Balance Equation for this Geometry Gives:

\[ T(x) = -q''', \frac{x(x - L)}{2k} + T_s \]

So that

\[ \Delta T = -\frac{L^2}{8k} \Delta H_{\text{overall}} \frac{\rho_{\text{Hydride}}}{M_{\text{Hyd eff}} M_{\text{H₂}}} \frac{\Delta m_{\text{H₂}}}{\Delta t} \]

where:

\[ \Delta T = T_{\text{max}} - T_s \]
Steady-State Energy Balance

\[ \frac{1}{r} \frac{d}{dr} \left( r \frac{dT}{dr} \right) + q''' = 0 \]

\( q''' \) (W/m³) is the rate of thermal energy release during charging or discharging

\[ q''' = - \sum_i \Delta H_i \frac{\Delta C_i}{\Delta t} \]

where:

- \( \Delta H \) (J/mol) is the enthalpy of reaction
- \( C_i \) (mol/m³) is concentration of H₂ stored by species \( i \)
- \( C_f \) (mol/m³) is overall concentration of stored H₂
- \( M_{\text{Hyd}_\text{eff}} \) is the mass of hydride needed to store the required mass of hydrogen

Solving the Energy Balance Equation for this Geometry Gives:

\[ T(r) = T_s + \frac{q'''}{4k} \left[ -r^2 + 2r_2 r + \left( r_1^2 - 2r_1 r_2 \right) \right] \]

So that

\[ \Delta T = - \frac{L^2}{4k} \frac{\Delta H_{\text{overall}}}{M_{\text{Hyd}_\text{eff}} M_{H_2}} \frac{\Delta m_{H_2}}{\Delta t} \]

where:

\[ L^2 = r_1^2 - r_2^2 \]
Approach: Application & Interpretation of Acceptability Envelope

Media packing $\rightarrow \rho_{\text{Hydride}}$

Media kinetics & loading time $\rightarrow M_{\text{Hyd eff}}$ & $\Delta T$

Media thermal properties $\rightarrow k$

Loading rate from technical targets $\rightarrow$ Minimum value for

$$\min \left( \frac{1}{L^2} \left( \frac{k M_{\text{Hyd eff}} \Delta T}{-\Delta H_{\text{overall}} \rho_{\text{Hydride}}} \right) \right)$$

Media thermodynamics $\rightarrow \Delta H_{\text{overall}}$

Storage system mass and volume constraints $\rightarrow L, M_{\text{Hyd eff}}, \rho_{\text{Hydride}}, P \text{ (implicit in kinetics)}$

HSECoE
Approach: Acceptability Envelope Constraints Based on DOE Technical Targets

DOE Technical Targets

<table>
<thead>
<tr>
<th>Target</th>
<th>System Gravimetric Capacity</th>
<th>Hydride weight / System weight</th>
<th>(\Delta t) (min) for 5 kg (H_2)</th>
<th>(\Delta m_{H_2}/\Delta t) (kg/s)</th>
<th>(M_{Hyd_eff} [kg]) for 5 kg (H_2)</th>
</tr>
</thead>
<tbody>
<tr>
<td>DOE 2010 year</td>
<td>0.045</td>
<td>0.52</td>
<td>4.2</td>
<td>0.0198</td>
<td>58.1 ((\Delta t = 4.2) min)</td>
</tr>
<tr>
<td>DOE 2015 year</td>
<td>0.055</td>
<td>0.55</td>
<td>3.3</td>
<td>0.0253</td>
<td>50.0 ((\Delta t = 3.3) min)</td>
</tr>
<tr>
<td>DOE Ultimate target</td>
<td>0.075</td>
<td>0.60</td>
<td>2.5</td>
<td>0.0333</td>
<td>40.0 ((\Delta t = 2.5) min)</td>
</tr>
</tbody>
</table>

- Parametric analysis applied for fixed \(\Delta T\), \(\Delta H_{\text{overall}}\), \(\rho_{\text{Hydride}}\) and \(M_{\text{Hyd\_eff}}\) and varying:
  - Thermal conductivity, \(k\)
  - Spacing of heat transfer elements, \(L\)
Approach: Value of Parameter Grouping in Acceptability Envelope

Acceptability Envelope

\[
\frac{1}{L^2} \left[ \left( kM_{\text{Hyd eff}} \Delta T \right) / \left( -\Delta H_{\text{Overall} \rho_{\text{Hydride}}} \right) \right] \text{ vs Charging/Discharging Rate}
\]

\[
\frac{1}{m_{M_{\text{H}_2}}} \frac{\Delta m_{\text{H}_2}}{\Delta t}
\]

Rectangular Coordinates

Cylindrical Coordinates

\[
\Delta m_{\text{H}_2}/\Delta t \text{ (kg H}_2/\text{s)}
\]

Ultimate Target

2015 Target

2010 Target
Technical Accomplishments: Overall Summary

• **Have met the following Phase I objectives:**
  - Developed acceptability envelope for metal hydrides
    - *Need to specify gravimetric & volumetric constraints*
  - Performed comparison between metal hydride models & available data
  - Developed baseline models for metal hydrides
    - *Initiated model development for adsorbent media*
  - Performing optimization studies and modeling of vessel configurations

• **Detailed models**
  - Ready to compare storage system behavior for different media
    - Metal hydrides
    - Adsorbents MOF-5® and MaxSorb®

• **Acceptability envelope**
  - Metal hydrides
    - Applying to vessel-media configurations
  - Adsorbents
    - Model is being developed

• **Path forward:**
  - Continue sensitivity analyses
  - Pursue novel concepts
    - *Micro & mini-channel heat exchangers*
    - *Structured media*
  - Conduct preliminary system design